

A collective mechanism for phase variation in biofilms

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Understanding how microbes gather into biofilm communities and maintain diversity remains one of the central questions of microbiology, requiring an understanding of microbes as communal rather than individual organisms. Phase variation plays an integral role in the formation of diverse phenotypes within biofilms. We propose a collective mechanism for phase variation based on gene transfer agents, and apply the theory to predict the population structure and growth dynamics of a biofilm. Our results describe quantitatively recent experiments, with the only adjustable parameter being the rate of intercellular horizontal gene transfer. Our approach derives from a more general picture for the emergence of cooperation between microbes.

mobile genetic elements | horizontal gene transfer

From river rocks to tooth enamel, biofilms have insinuated themselves onto the world's surfaces (1, 2). Colonizing the surfaces of the world is no simple matter. It is widely held that a coordinated effort from many types of contributors that often involves sacrifices made by individual cells is required. Biofilms are a heterogeneous aggregation of microbial phenotypes (3, 4) that live together as a community, coordinating group activities, such as circulation, dispersion, and aggregate movement (5–9). The different types of cells rely on each other, so that their mutual interactions lead to the overall success of the group.

This coordinated group behavior within a microbial community is frequently referred to as “multicellular behavior” (10–13) to emphasize the importance of considering the structure of the community over the individual. Can local interactions between members of the community lead to global coordinated behavior of the biofilm? To address these issues in concrete terms, we show here that simple interactions between microbes mediated by mobile genetic elements (MGEs) (14–16) can explain quantitatively the important phenomena of phase variation (17, 18).

Phase variation is the phenomenon in which a single microbial biofilm changes its behavior and differentiates into several phenotypes. Given the central role different phenotypes play in the overall success of a community, phase variation is naturally central to the nature of biofilms. Phase variation has been found to occur via many different mechanisms (19–21), many of which are variations on a common theme of genetic rearrangements. Although most of the literature on phase variation focuses on internal rearrangements within a cell (19, 20), phase variation has also been documented to occur via interactions with genetic elements from outside of the cell (22). It has even been proposed that mobile genetic elements such as bacteriophage μ may have been the evolutionary precursors to phase variation by an internal genetic rearrangement (19).

The purpose of this article is to propose a minimal model by which MGEs acting between microbial genomes can bring about the phenomena of phase variation through a collective mechanism. Our model predicts that organisms within a biofilm have the inherent capacity to change their phenotypes, and that these phenotypes can stably coexist. We also examine the dynamics of phase variation and demonstrate that our model predicts features observed in experimental data on the formation of variants in biofilm cultures. For comparison with the available experimental data, the model solved here has been constructed with single organism biofilms in mind. However, in nature, biofilms

often contain a plurality of species (12, 23). The theory presented here is not restricted to single organism biofilms but can be generalized to model multispecies biofilms.

The structure of this article is as follows: First, we review the phenomena of phase variation. We briefly mention various mechanisms for phase variation and focus on the examples that may best be explained by our model or that offer a precedent for our model. Next, we describe the statistical mechanics of horizontal gene transfer (HGT) and compute the steady states of our model, exhibiting in particular the coexistence of phenotypes. We use the model to simulate the population dynamics of biofilms and find that we are able to account for the key features of the available experimental data. We conclude by discussing our results and their broader implications for microbial ecosystems.

Evidence for the Participation of Mobile Genetic Elements

Microbes linked together into a biofilm often give rise to phenotypic diversity through the phenomena of phase variation. Phase variation has been defined as “oscillations in phenotype” or “on-off” switches in phenotype (24, 25). Both of these definitions capture the same element of sudden change in phenotypic characteristics, usually at a relatively high rate compared with other genetic mechanisms such as point mutations (20, 26). A review of how phase variation fits into the larger scheme of variation-producing mechanisms, especially with regard to frequency and time scales, is given in ref. 26.

The switching mechanism in phase variation often involves genetic rearrangements, such as inverted segments of DNA (19), mobile transposons (21), or expression of silent genetic material through homologous recombination (20). We now briefly highlight some examples of these phase variation mechanisms. *Staphylococcus epidermidis* is capable of forming variants that produce a polysaccharide intercellular adhesin (PIA) important in the formation of thick, multilayered biofilms. According to Zeibuhr *et al.* (21), the cause of 30% of the PIA-negative variants was found to be the insertion of insertion sequence element 256 (IS256) into and the subsequent inactivation of either the *icaA* or *icaC* genes. Furthermore, insertion of IS256 was found to be reversible and upon excision of IS256 the PIA phenotype was restored.

Koomey *et al.* (20) found that in *Neisseria gonorrhoeae* homologous recombination between a pilus gene in an actively expressed locus and several partial copies of pilus⁺ and pilus⁻ genes in silent storage loci drive the phase variation. Recombination with the different silent loci makes changes to the expressed pilus gene and thus changes the phenotype of the cell. In reverse, recombination events that return the gene to its previous form restore the former phenotype as well. Inactivation

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of *recA* leads to a 100- to 1,000-fold lower frequency of phase variation.

Although the particulars of these mechanisms may involve differing molecular reactions and pathways, they share two general features. First, they are reversible gene mutations for inducing a phenotypic change by genetically altering expression levels or the expressed products themselves. These mechanisms conserve the genetic material that causes the change. This conservation is an important factor in the heritability and stabilization of the phase variation behavior across generations. The stochastic nature of these genetic rearrangements, wherein each reaction possesses a forwards and a backwards rate and is in principle a chemical equilibrium, allows for the stable coexistence of phenotypes at consistent ratios—an important feature in natural biofilms and one that allows us to obtain reproducible experimental results that can be compared with theoretical predictions.

The second feature that these mechanisms share is that they involve solely internal genome rearrangements. However, it is known that microbes are not restricted to interacting with only their own genetic material. MGEs such as raw DNA, transposons, plasmids, and viruses, are capable of introducing external genetic material into a microbe (2, 14, 15, 16, 27). This external genetic material can then insert into or recombine with the cellular genome. MGEs can carry functional genes between organisms as in the case of HGT. MGEs can also integrate into a gene or its promoter region causing a disruption in that gene's expression. These mechanisms are similar to those of phase variation via internal genetic rearrangements (20, 21). The main difference is the communal nature of the rearrangements in the case of the MGEs. The MGEs allow for the exchange of genetic material between microbes whereas the internal genetic rearrangements do not.

Webb *et al.* (28) found that cells from a strain of *Pseudomonas aeruginosa* exposed to filamentous bacteriophage Pf4 underwent phase variation, switching to a small colony variant (SCV) phenotype. This bacteriophage is naturally associated with the strain of *P. aeruginosa* studied. The SCVs displayed the phenotypic traits of enhanced attachment. A common theme for biofilm development, enhanced attachment plays a crucial role in the dense packing, structure, and adherence of cells to the biofilm (3). Resch *et al.* (29) found spontaneous release of lysogenic phages in *Staphylococcus aureus* and postulated that phages are an important part of the biofilm state, playing a role in persistence and survival. Bacteriophages have been shown to regulate genes in *Escherichia coli* (30), leading to a change in host phenotype. While the precise nature of the interactions between viruses and biofilms is not clear, they appear to be an important part of the community dynamics.

Neisseria gonorrhoeae, as mentioned previously, has both an expression locus and silent storage loci that recombine, giving rise to phase variation (20). Transformation and recombination are known to play a large role in *Neisseria*. These pathogens are naturally competent, always ready to take up exogenous DNA from their environment. Furthermore, it was found that transformation, the act of taking up exogenous DNA from lysed cells, can increase the rate of phase variation. This rate increases most when the DNA that is taken up comes from a related but different strain of *Neisseria* (31). It is known that titration of the slip-strand repair proteins *mutS* and *mutL* play a role in increasing rate of phase variation by effectively increasing the rate of mutations. However, increasing the chemical concentrations of *mutS* and *mutL* only lessens the increase in the rate of phase variation, but does not eliminate it, raising the possibility of another mechanism acting in conjunction with the mismatch repair saturation (31, 32). Alexander *et al.* (31) wrote that “the other mechanism must also require DNA entry into the cell and a functional *recA* allele, because transformation and recombi-

nation deficient meningococci were not altered in their phase variation.” Additional recombination between the exogenous *Neisseria* DNA and the expression locus is one such possible mechanism for increasing the rate of phase variation (33).

Finally, conjugative DNA exchange and recombination has been observed in the genome of the hyperthermophile archaeon *Sulfolobus acidocaldarius* (34, 35). DNA exchange in *S. acidocaldarius* may not only serve as a mechanism for phase variation, but as a means for conjugative DNA repair (34).

Smith has shown that MGEs can serve to maintain certain types of cooperative behavior between microbes (36). When the benefits of virulence factors are shared by all members, and dependent on the total communal production of the virulence factor, MGEs horizontally transfer the virulence factor genes through members of the community. The communal nature of MGEs then drives the evolution of communal MGE-associated virulence factor genes, examples of “cosmopolitan genes” (37)—specialty genes whose presence is dictated by the environment, and are thus more characteristic of the environment than of a single organism.

In summary, even a biofilm grown from a single microbe is capable of producing a community consisting of several variant phenotypes, a phenomenon that is an important component for the survival and persistence of biofilms in general (38). Phase variation is the mechanism by which many of these different phenotypes are produced. This mutationally generated phenotype switch is reversible and inheritable. Genetic rearrangements are capable of causing a change in phenotype and are often the means through which a microbe switches phenotype, either within a cellular genome or through MGEs acting between cells (28, 33).

Minimal Model for Mobile Genetic Element Mediated Phase Variation

To model phase variation mediated by horizontal gene transfer, our strategy is to extract the features common to all of the molecular mechanisms of genome rearrangement described above, as is described in refs. 39 and 40, even though we fully recognize that there are specific case-by-case variations. The end result of any gene transfer mechanism is the simple transfer of genes between cells. Particulars may differ, but the main effects are the same. In each of these systems, there is at least one actively expressed locus that is responsible for phenotype. Changes in the genetic material at this locus result in a change in phenotype or phase variation. In addition, there is usually a means of preserving the inactive genetic material. For example, in the case of intragenomic recombination, inactive genetic material in the form of partial copies of a gene was stored in several unexpressed storage loci (20).

Because these shared general features are likely to exist in some way in a broad class of genetically mediated phase variation systems, we can construct a generic minimal model for describing the main features of all MGE-mediated phase variation systems. In this model exist two phenotypes labeled 0 and 1. There are two types of gene, 0 and 1, each corresponding to a phenotype. A microbial cell contains a genome with two genes in two loci: an active expressed locus gene α and an inactive storage locus gene β . The phenotype of a given microbe is given by the gene in the active locus. The gene at the storage locus has no effect on the phenotype of the microbial cell. We denote the four possible microbial genome types by the indices $\alpha\beta$. The first index denotes the gene at the active locus while that second index denotes the gene in the storage locus. The four different possible microbial genomes are in this notation: 00, 01, 10, and 11. $\psi_{\alpha\beta}$ denotes the number of microbes with genome $\alpha\beta$. The first two types of microbes, ψ_{00} and ψ_{01} , express the 0 phenotype, while the last two, ψ_{10} and ψ_{11} , express the 1 phenotype. The composition of

the microbial community is represented by the relative abundances of each of the four microbial genomes.

The microbes within the community are capable of interacting with the MGEs of the community. An individual microbe may take in an external gene x from the shared gene pool of the community. That gene can recombine with the active locus with a certain probability q_x or with the storage locus with a probability $1 - q_x$. The site-specific probability of recombination depends on the type of gene that enters the microbe. The external gene comes from a community gene pool whose composition is a direct reflection of the composition of the cellular genomes. In other words, the chance of getting a 0 gene is $p_0 = (2\psi_{00} + \psi_{01} + \psi_{10}) / (2\psi_{\text{total}})$, where $\psi_{\text{total}} = \psi_{00} + \psi_{01} + \psi_{10} + \psi_{11}$. Conversely, the probability of getting a 1 gene is $1 - p_0$.

Phase variation, or phenotype switching, occurs when the active locus in a genome is overwritten with a gene for a different phenotype. For example, if a 1 gene enters into a microbe with a 00 genome and overwrites the active locus subsequently transforming it into a 10 genome, then that microbe has undergone a switch from a 0 phenotype microbe to a 1 phenotype microbe.

One of the common and important features of biofilms and phase variation is the emergence of a steady-state ratio of phenotypes after the culture reaches stationary state. This is no doubt important for preserving variety, i.e., preventing all cell types from switching to variant types, and enforcing some advantageous fractions of coexistence between phenotypes. Because different phenotypes play different roles within a microbial community, there is a particular ratio of role players that is most efficient and effective for the maintenance, survival, growth, and dispersal of the biofilm.

To understand the steady state ratio of phenotypes, we normalize the total number of microbes so that $\psi_{\text{total}} = 1$. $\psi_{\alpha\beta}$ then gives the fraction of the population with the genome $\alpha\beta$. Because our purpose is to examine the stationary state, we do not allow cellular growth or death. Only gene transfers drive the system. The two parameters of this system are q_0 and q_1 , the probabilities of each type of gene recombining with the active locus. The time-dependent dynamics of the system are then given by the equation

$$\frac{1}{r} \frac{\partial \psi_{00}}{\partial t} = p_0(1 - q_0)\psi_{01} + p_0q_0\psi_{10} - p_1\psi_{00} \quad [1]$$

$$\frac{1}{r} \frac{\partial \psi_{01}}{\partial t} = p_1(1 - q_1)\psi_{00} + p_0q_0\psi_{11} - (p_0(1 - q_0) + p_1q_1)\psi_{01} \quad [2]$$

$$\frac{1}{r} \frac{\partial \psi_{10}}{\partial t} = p_1q_1\psi_{00} + p_0(1 - q_0)\psi_{11} - (p_1(1 - q_1) + p_0q_0)\psi_{10} \quad [3]$$

$$\frac{1}{r} \frac{\partial \psi_{11}}{\partial t} = p_1q_1\psi_{01} + p_1(1 - q_1)\psi_{10} - p_0\psi_{11}, \quad [4]$$

where r is the rate of intercellular horizontal gene transfer. The terms in these equations describe, within mean-field theory, the processes of gene transfer; for example, the probability of going from a 00 genome to a 10 genome depends on the probability of obtaining a 1 gene from the gene pool p_1 and having that gene recombine with the active site q_1 . This particular sequence of events carries a total probability of $p_1q_1 = (1 - p_0)q_1$. Although these equations can be derived as moments from a master equation formalism, we expect that in a biofilm environment, fluctuations are small, and the mean field approximation is reliable. The steady state is then given by the fixed point transfer matrix equation

$$\psi = \hat{T}\psi, \quad [5]$$

where Ψ is a vector whose components are ψ_{00} , ψ_{01} , ψ_{10} , and ψ_{11} , and \hat{T} is a transfer matrix

$$\hat{T} = \begin{pmatrix} p_0 & p_0(1 - q_0) & p_0q_0 & 0 \\ p_1(1 - q_1) & p_0q_0 + p_1(1 - q_1) & 0 & p_0q_0 \\ p_1q_1 & 0 & p_1q_1 + p_0(1 - q_0) & p_0(1 - q_0) \\ 0 & p_1q_1 & p_1(1 - q_1) & p_1 \end{pmatrix} \quad [6]$$

whose elements describe the transition probabilities given a gene pool matching the composition of the cells. This steady state condition can be derived from the time-dependent equations, because all transition probabilities must sum to unity.

Results

Steady States. Stable steady state solutions for Eq. 1 with coexisting phenotypes only exist for the conditions $0 < q_x < 1/2$ and $1/2 < q_y < 1$ where (x, y) are $(0, 1)$ or $(1, 0)$. In other words, each gene must have a different primary site for recombination. Otherwise the resulting competition leads to the eventual fixation of one gene to the exclusion of the other, and no stable coexistence can occur. The coexisting fraction of 0 phenotype microbes p_0 can be found by solving Eq. 1, yielding

$$p_0(q_0, q_1) = \psi_{00} + \psi_{01} = \frac{q_0 - 2q_0q_1}{q_0 - q_1}. \quad [7]$$

This equation describes the steady state coexistence for the zero growth and equal transfer rates for both types of genes. For $0 < q_x < q_y < 1/2$ or $1/2 < q_y < q_x < 1$, gene x saturates all loci in the system completely excluding gene y . Also, $0 < q_0 = q_1 < 1$ results in an unstable equilibrium. Fig. 1 shows the phase diagram and a diagrammatic representation of the stability of the fixed points in both the single and coexistent phenotype phases. In the singular phase, the population fractions flow toward all 00- or 11-genotypes and away from any intermediate values. The coexistent phase is characterized by an attractive fixed point given by the solution to Eq. 1. For example, the fixed point drawn in Fig. 1 would be given by

$$\psi_{00} = \frac{(1 - q_0)q_0(1 - 2q_1)^2}{(q_0 - q_1)^2} \quad [8]$$

$$\psi_{01} = \frac{(2q_0 - 1)q_0(1 - 3q_1 + 2q_1^2)}{(q_0 - q_1)^2} \quad [9]$$

$$\psi_{10} = \frac{(1 - q_1)q_1(1 - 2q_0)^2}{(q_0 - q_1)^2} \quad [10]$$

$$\psi_{11} = \frac{(1 - q_1)q_1(1 - 2q_0)^2}{(q_0 - q_1)^2}. \quad [11]$$

In Fig. 2, we show how the phenotype fraction varies with q_0 and q_1 , exhibiting the way in which the family of curves conveniently collapse onto a universal curve when plotted in the manner specified by Eq. 1.

Dynamics. We have shown how stable coexistence of two phenotypes can arise via the mechanism of gene transfer. In this section, we wish to further examine the dynamics of gene transfer for changing populations of microbes. Thus, we will consider the role of both initial conditions and microbial growth.

Consider the onset of variant phenotypes in biofilm cultures. Although natural biofilms can comprise, with attendant genetic exchanges, a variety of microbial types, their phenotypic behavior can be conveniently studied using a single organismal strain. Typically, a biofilm reactor is inoculated with cells from a

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Supporting Information

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SI Text: Details of Simulation Results in Figs. 3 and 4

Simulating the dynamics of the MGE-mediated phase variation follows closely along the lines described in *Minimal Model for Mobile Genetic Element Mediated Phase Variation* in the main text. In particular, the simulations were discrete time, finite population size implementations of master equations, which reproduce Eqs. 1–4 in the infinite population limit. While the more analytically tractable Eqs. 1–4 are more appropriate for describing continuous time, infinite population dynamic, the simulations were carried out with a finite resource limit and discrete cells to more directly represent the discrete interactions acting on individual cells. Individual microbes are represented by a genome containing two loci—an active locus and an inactive locus. The gene in the active locus determines the phenotype of the cell, which is represented as a 0 or 1. Likewise, genes are also represented by a 0 or 1, corresponding to the resulting phenotype when the gene is in the active locus. The population of microbes is represented by an array of genomes where the size of the array represents the carrying capacity or maximum size of the system. Each element of the population array can take one of five states: 00, 01, 10, 11, or “empty.” The first four states represent the genes in the two loci genome starting with the gene active locus. The last state indicates that there is no cell occupying this position in the array.

Simulations were conducted by iterating the following steps:

1. Growth. Cells for replication are selected at random. The base rate of replication depends on the lesser of two quantities, either the number of cells, or the difference between the carrying capacity of the system and the number of cells. In any case, half the lesser number determines the base rate of replication. These rates correspond to exponential growth in the small population limit, and logarithmic growth up to the carrying capacity of the system in the large population limit. The base rate is then multiplied by a factor that controls the size of the individual time steps, in this case 0.25. For a non-integer number of replication events, an extra replication event occurs sometimes according to the appropriate probability. In Fig. 4, where the cell types exhibit different attachment rates, this is simulated by using unequal growth rates for each phenotype. In this case, a fraction of the randomly selected slower growers do not replicate according
2. Gene transfer. A random gene is selected from the population of microbes. This could represent a direct exchange between two microbial cells. Likewise, this also could be considered an approximation of genetic uptake from a communal gene pool, whose composition approximately reflects the genes within the cellular genomes. The selected gene then is paired with a randomly selected cell. The gene then overwrites the active locus according to the probability q_0 or q_1 or the inactive locus with a probability of $1 - q_0$ or $1 - q_1$, depending on whether the gene is a 0-gene or a 1-gene. The number of these gene transfer events is determined according to the number of cells in the population, multiplied by a rate of gene transfer (chosen to be $\frac{3}{4}$ for Figs. 3 and 4) and the same factor of 0.25 that indicates the size of each time step in the simulation.

To make the gene transfer rate the only unconstrained parameter of this model, we use two pieces of data. First, we used the growth curve in Fig. 3 to determine the rate of replication. For the experiment in Fig. 4, where we lacked this data, we used a similar overall growth rate as used in Fig. 3, but with a 0-phenotype to 1-phenotype growth rate ratio of 0.85. Anchoring the growth rate to experimental data allows us to frame the gene transfer rate in terms of transfers per replication in the exponential growth phase. To set the other parameters, we choose q_0 and q_1 such that they are consistent with the coexistence ratio of the two phenotypes 0 and 1 for the final experimental time point, i.e., we match the steady state ratio of phenotypes, in Fig. 3. Note that there may be multiple values of q_0 and q_1 that result in the same phenotype coexistence ratio. However, simulation results remain remarkably similar for any choice made matching the steady state constraint.

Last, initial conditions are chosen based on the simulated steady state distribution of genotypes. That is to say, for Fig. 3, where the culture is inoculated by a single phenotype, the ratio of genotypes in the initial population is given by the ratio 00:01. For Fig. 4, where the inoculum contains both 0 and 1 phenotypes, the ratio of genotypes for each phenotype is given according to the steady state ratios 00:01 and 10:11, respectively.